

density, $\tilde{\rho}_\alpha$. No relation such as Equation (37) can be obtained for the constituent compression in the physical configuration, $\tilde{\rho}_\alpha/\tilde{\rho}_{\alpha 0}$. When \hat{c}_σ^α is not zero, Equation (37) must be replaced by

$$\eta_\alpha = \eta \left(1 + \frac{\hat{c}_\sigma^\alpha}{\rho_{\alpha 0} U} \right) \quad (38)$$

We can now investigate the question of a phase transformation in one of the constituents. Suppose constituent S_1 transforms into constituent S_2 at shock pressures in excess of \tilde{P}^* . We assume that no S_2 is initially present leading the shock. That is

$$\rho_{20} = 0 \quad (39)$$

We assume that, following the shock, all of constituent S_1 has been transformed to S_2 so that

$$\rho_1^- = 0 \quad (40)$$

Using Equation (40) in Equation (25), we obtain

$$\hat{c}_\sigma^1 = -\rho_{10} U, \quad \text{for } \tilde{P}_\alpha^- \geq \tilde{P}^* \quad (41)$$

while use of Equation (39) in Equation (25) gives

$$\hat{c}_\sigma^2 = \rho_2^-(U - v^-), \quad \text{for } \tilde{P}_\alpha^- \geq \tilde{P}^* \quad (42)$$

Then, if no other mass exchange occurs, Equation (13) implies that

$$\rho_2^-(U - v^-) = \rho_{10} U \quad (43)$$

whenever \tilde{P}_α^- exceeds the transformation pressure, \tilde{P}^* . In this case, we have

$$\frac{\rho_2^-}{\rho_{10}} = \eta_3 = \eta_4 = \dots = \eta_k = \eta \quad (44)$$

More complex interactions, including chemical reactions among constituents within the shock surface, can be treated in a similar manner. It is necessary only to assume constitutive relations for the supplies, \hat{c}_σ^α , obeying Equation (13).

Next, we turn to the physical configuration and assume that the constituent crystal pressures, \tilde{P}_α^- , are all equal, provided S_α exists behind the shock. That is

$$\tilde{P}_\alpha^- = \tilde{P}^-, \quad \text{for all } \alpha \text{ such that } \rho_\alpha^- \neq 0 \quad (45)$$

Then Equations (23) and (30), together with this assumption, imply that

$$P^- = \tilde{P}^- \quad (46)$$

That is, the total mixture pressure must equal the crystal pressure in each constituent. The momentum jump equation [Equation (26)] can then be written as

$$n_{\alpha}^- \tilde{P}^- + m_{\sigma} = \rho_{\alpha}^- (U - v^-) v^- \quad (47)$$

Summing this equation over α and using Equations (14) and (16), we obtain the usual momentum jump equation for the whole mixture.

$$\tilde{P}^- = \rho^- (U - v^-) v^- \quad (48)$$

Our assumptions of equal particle velocities and equal crystal pressures in all extant constituents have implied the form of the momentum supply functions, $\hat{m}_{\sigma}^{\alpha}$. Eliminating the quantity $(U - v^-) v^-$ between Equations (47) and (48) yields

$$\hat{m}_{\sigma}^{\alpha} = \tilde{P}^- (c_{\alpha}^- - n_{\alpha}^-) \quad (49)$$

where c_{α}^- is the concentration ρ_{α}^-/ρ^- following the shock. Using Equation (38), we can write c_{α}^- as

$$c_{\alpha}^- = c_{\alpha 0} \left(1 + \frac{\hat{\sigma}_{\alpha}}{\rho_{\alpha 0} U} \right) \quad (50)$$

Note that, if no mass transfer occurs, the concentration will not change crossing the shock.

The energy balance relation, Equation (27), may also be simplified by these assumptions. If S_{α} does not vanish behind the shock, we can divide Equation (27) by the volume fraction, n_{α}^- , to obtain

$$\tilde{P}^- v^- + \frac{\hat{\sigma}_{\alpha}}{n_{\alpha}^-} = \tilde{p}_{\alpha}^- (U - v^-) \left(e_{\alpha}^- + \frac{1}{2} (v^-)^2 \right) + \tilde{h}_{\alpha}^- \quad (51)$$

where Equations (17), (19), (23), (28), and (45) have all been used. Also, summing Equation (27) over α and taking Equations (15), (30), (31), and (32) into account, we obtain the usual energy jump equation for the whole mixture.

$$\tilde{P}^- v^- = \rho^- (U - v^-) \left(\epsilon^- + \frac{1}{2} (v^-)^2 \right) + h^- \quad (52)$$

We point out here that the constituent heat flux, h_{α}^- , does not account in any way for transfer of heat between constituents. The action of h_{α}^- is entirely restricted to S_{α} . Heat may be transferred among the constituents, however,